

# SMALL AND MEDIUM SIZED LIQUID METAL COOLED SAFETY ANALYSIS USING MULTI LEVEL COMPLEXITY MODEL

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## Abstract

SMALL AND MEDIUM SIZED LIQUID METAL COOLED SAFETY ANALYSIS USING MULTI LEVEL COMPLEXITY MODEL Inherent safety characteristics of liquid metal cooled fast reactors is very important capital for next generation nuclear power plants. However inherent safety assessment need appropriate computer code or experiment. Here, a computer code for liquid metal cooled fast reactor accident analysis with various level of complexity has been developed. At the simplest approach, quasi-static method is adopted to get asymptotic condition during UTOP, ULOF, and UTOP-ULOF accident. Here we can get asymptotic power level, asymptotic average coolant temperature, and asymptotic fuel temperature for a certain external reactivity and natural circulation level. In the next grade, the code will simulate transient effect using point kinetic method and quasistatic approach for thermal hydraulic analysis. Here we can get time dependet power change, coolant temperature change and fuel temperature change. Finally in the rigorous analysis, coupled space dependent kinetic and transient thermal hydraulic are coupled and solved to get time dependet information of various process involved in the accident.

Keywords : Accident, ULOF, UTOP, reactivity, feedback, quasistatic, space-depedent kinetic.

## Abstrak

**ANALISIS KESELAMATAN REAKTOR BERPENDINGIN LOGAM CAIR UKURAN KECIL DAN MENENGAH MENGGUNAKAN MODEL KOMPLEKSITAS MULTI LEVEL.** Karakteristik keselamatan inheren dari reaktor cepat berpendingin logam cair merupakan modal yang sangat penting bagi pembangkit listrik nuklir generasi mendatang. Namun, penilaian keselamatan inheren membutuhkan kode komputer atau eksperimen yang sesuai. Di sini, kode computer untuk analisis kecelakaan reactor cepat berpendingin logam cair dengan berbagai tingkat kompleksitas telah dikembangkan. Pada pendekatan yang paling sederhana, metode quasi-statis diterapkan untuk memperoleh kondisi asimptotik selama kecelakaan UTOP, ULOF, dan UTOP-ULOF. Kita bisa mendapatkan tingkat tenaga asimptotik, suhu pendingin rata-rata asimptotik, dan suhu bahan baker asimptotik untuk tingkat sirkulasi alami dan reaktivitas eksternal tertentu. Pada tahap berikutnya, kode tersebut akan mensimulasi efek transien menggunakan metode point-kinetik dan pendekatan quasistatik untuk analisis hidraulik thermal. Kita bisa memperoleh perubahan daya tergantung waktu, perubahan suhu pendingin, dan perubahan suhu bahan baker. Akhirnya, dengan analisis yang teliti, kinetic tergantung ruang berpasangan dan hidrolik thermal transien dipasangkan dan diselesaikan untuk mendapat informasi tergantung-waktu dari berbagai proses yang terlibat dalam kecelakaan tersebut.

Kata kunci : Kecelakaan, ULOF, UTOP, reaktivitas, umpan balik, quasistatic, space-depedent kinetic.



## INTRODUCTION

TMI-2 and Chernobyl accidents have pushed the safety paradigm of nuclear reactors toward inherent/passive safety. For liquid metal cooled fast reactors, proper combination of reactivity feedback will result in inherent safety capability against unprotected rod run out transient over power (UTOP) accident and unprotected loss of flow (ULOF) accident (Su'ud and Sekimoto, 1995; Su'ud and Sekimoto, 1996; Su'ud, 1998; Su'ud, 2003; Su'ud, 2004a; Su'ud, 2004b; Su'ud, 2004c; Su'ud, 2004).

During unprotected rod runout transient over power (UTOP) accident, reactor power increases due to external reactivity causing the increase of coolant and fuel temperature which induce overall negative reactivity feedback from doppler, radial expansion, axial fuel expansion and coolant density effect. The asymptotic equilibrium condition occurs when the negative reactivity feedback completely compensates external positive reactivity (Su'ud and Sekimoto, 1996; Su'ud, 2004).

In case of unprotected loss of flow (ULOF) accident, the loss of pumping power causes decrease of coolant flowrate. In the short term it causes the increase of coolant temperature but the decrease of fuel-coolant temperature difference. In asymptotic equilibrium condition, the negative reactivity due to the increase of coolant temperature is compensated by positive reactivity due to fuel temperature decrease in reduced power condition (Su'ud and Sekimoto, 1996; Su'ud, 2004).

Therefore UTOP and ULOF accident have different inherent defence mechanism and optimal characteristics are needed to survive both UTOP and ULOF accidents. In conventional LWR and MOX based liquid metal cooled fast reactors the temperature difference between fuel pin outer surface and pin center temperature can reach more than 1500°C. On the other hand, natural circulation level is very small (less than 10% of full power). Therefore during ULOF accident severe condition occurs, the decrease of power level to match natural circulation level will cause large positive reactivity due to doppler which can not be compensated safely by coolant temperature increase based negative feedback.

Here for special condition, i.e. relatively low power density and relatively large natural circulation capability (more than 20% of full power) we can reduce temperature difference between fuel pin outer surface temperature and fuel center temperature. Therefore we found that MOX based Pb-Bi cooled fast power reactors can survive ULOF accident inherently.

### Quasistatic Model

In UTOP accident, the positive reactivity drives the power increase, which in turn causes coolant, cladding and fuel temperature increase. The temperature increase draws negative reactivity feedback which compensates the external reactivity. In asymptotic condition the nuclear reactor will be in new stable condition with higher power level.

IN ULOF accident the unbalance between the heat source and the flowrate causes temperature increase in coolant, cladding and fuel which then cause negative

reactivity feedback. The negative reactivity feedback is then push the power down. At asymptotic condition the nuclear power will be stable in reduced power level.

### 1. Quasistatic Model Description

The basic model of Quasistatic approach is shown in the following figure

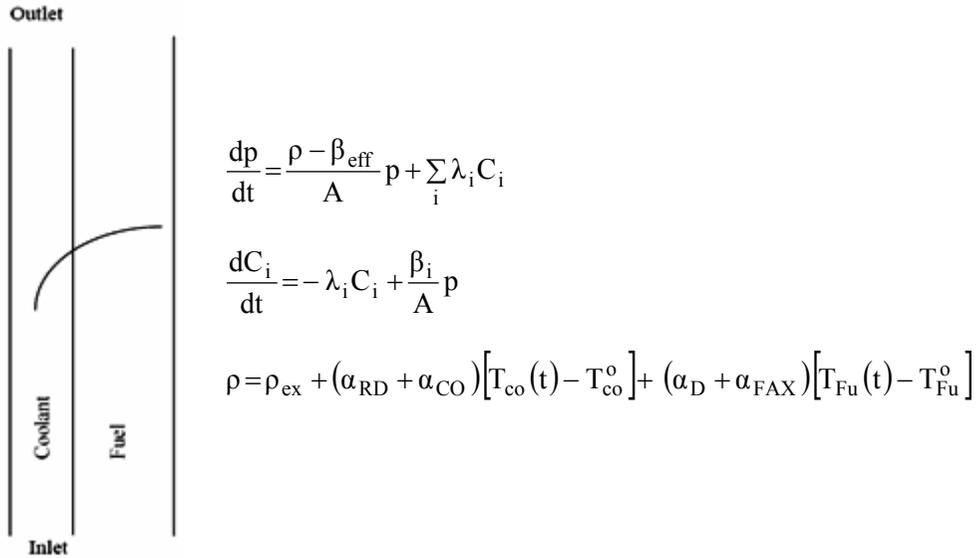


Fig. 1. Quasistatic safety analysis model for liquid metal cooled fast reactors

The coolant average temperature, coolant outlet temperature, coolant-fuel temperature difference, and fuel temperature average are expressed as follows.

$$T_{co,av} = \frac{T_{in} + T_{out}}{2}$$

$$T_{out} = T_{in} + \frac{p P_o A_{pin} H}{f(t) F_o C_p}$$

$$T_{co,av} = T_{in} + \frac{p P_o A_{pin} H}{2 f(t) F_o c_p}$$

$$\Delta T_{co, fu} = \frac{p P_o A_{pin} H R}{k_{fu} 2 \pi R H B} = \frac{p P_o A_{pin}}{2 \pi k_{fu} B}$$

$$T_{fu,av} = T_{co,av} + \Delta T_{co,fu} = T_{in} + \frac{p P_o A_{pin}}{2 \pi k_{fu} B}$$

where,  $f(t)$  is flow rate change with time (relative to initial flow-rate), and  $p(t)$  is power change with the time after accident (relative to initial power), and  $B$  is a parameter to adjust the model which in this case was set to 0.8.

## 2. Utop-ulof accident simulation using quasistatic model

Using the above description the model for UTOP and ULOF accidents can be described in more detail as follows. At the early stage after accident begin, the power increases due to external positive reactivity, and also the flow-rate decreases due to the coast down of the pumping power. Therefore the coolant and fuel temperature increases due to un-balanced between the heat source and the flow-rate. With the increase of the coolant and fuel temperature then negative feedback occurs and this will continue till this feedback is large enough to compensate external reactivity and to push down the power level to harmonize with the natural circulation level of the flow-rate. At the asymptotic level we will find that the flow rate is in natural circulation level while the power is adjusted to balance the natural circulation level so that the reactor will be in new equilibrium condition. At that time we have.

$$\rho = 0 = \rho_{ex} + (\alpha_D + \alpha_{FAX}) [T_{\infty}(t) - T_{\infty}^o] + (\alpha_D + \alpha_{FAX}) [T_{Fu}(t) - T_{Fu}]$$

$$0 = \rho_{ex} + (\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{\infty}) [T_{\infty}(t) - T_{\infty}^o] + (\alpha_D + \alpha_{FAX}) [\Delta T_{Fu,\infty}(t) - \Delta T_{Fu,\infty}^o]$$

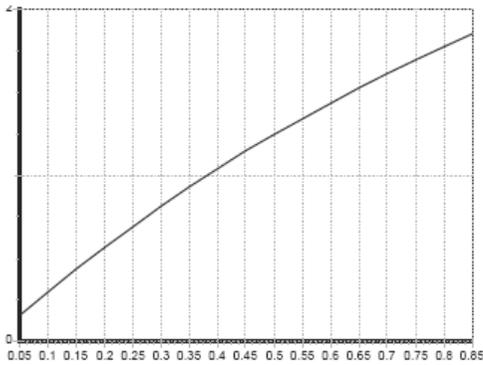
$$0 = (\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{co}) \left[ \frac{p}{f} - 1 \right] \frac{P_o A_{pin} H}{2 F_o C_p} + (\alpha_D + \alpha_F)$$

$$p \left[ (\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{co}) \frac{P_o A_{pin} H}{2 f F_o C_p} + (\alpha_D + \alpha_{FAX}) \frac{P_o A_{pin}}{2 \pi k_{Fu} B} \right]$$

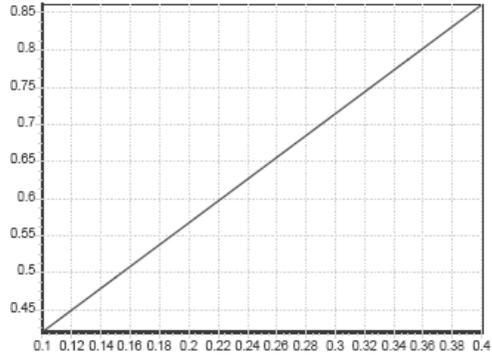
$$= (\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{co}) \frac{P_o A_{pin} H}{2 f F_o C_p} + (\alpha_D + \alpha_{FAX}) \frac{P_o A_{pin}}{2 \pi k_{Fu} B}$$

$$p = \frac{(\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{co}) \frac{P_o A_{pin} H}{2 f F_o C_p} + (\alpha_D + \alpha_{FAX}) \frac{P_o A_{pin}}{2 \pi k_{Fu} B} - \rho_{ex}}{(\alpha_D + \alpha_{FAX} + \alpha_{RD} + \alpha_{co}) \frac{P_o A_{pin} H}{2 f F_o C_p} + (\alpha_D + \alpha_{FAX}) \frac{P_o A_{pin}}{2 \pi k_{Fu} B}}$$

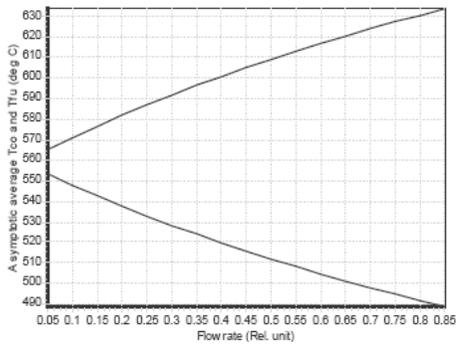
The example of simulation results is shown in the following figure.



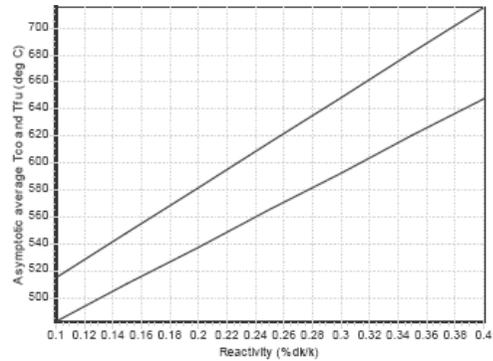
UTOP-ULOF Nitride +0.002



UTOP-ULOF Accident of Nitride Fuelled with f = 0.2

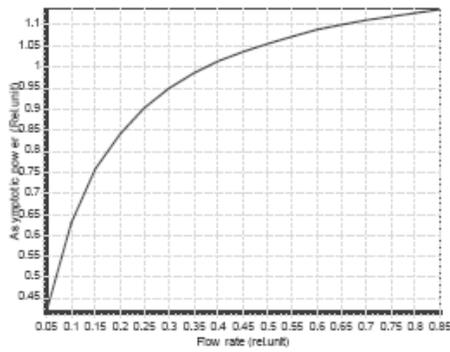


UTOP-ULOF Accident of Nitride Fuelled with f = 0.2

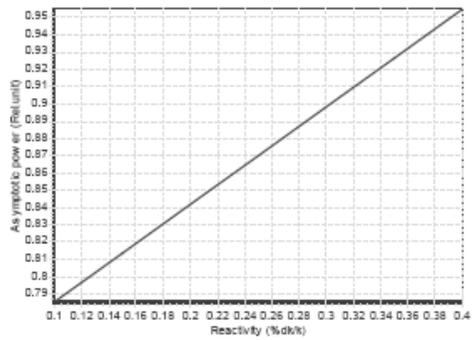


UTOP-ULOF Accident of Nitride Fuelled with f = 0.2

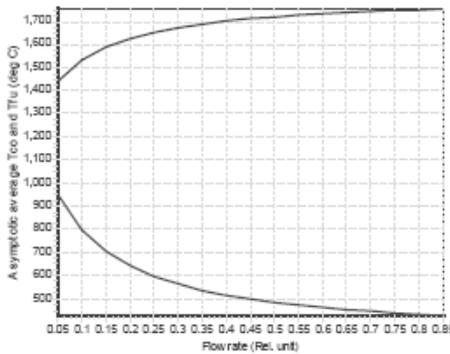
Fig. 2. ULOF-UTOP Accident for Nitride Fuelled Core



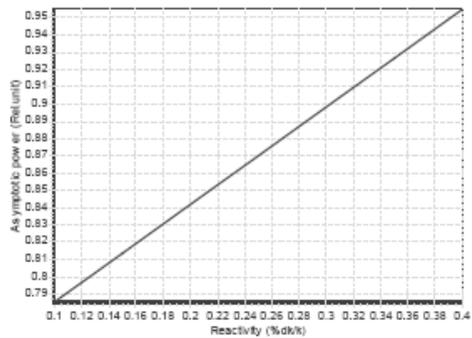
UTOP-ULOF Accident of Nitride Fuelled with  $\beta = 0.2$



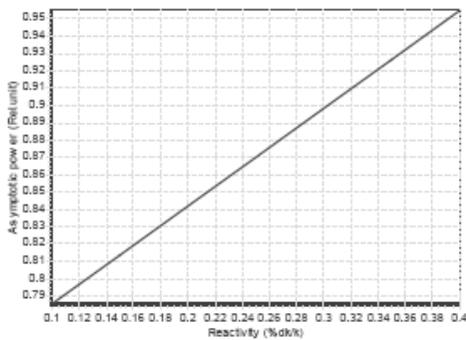
UTOP-ULOF, MOX FUEL with natural Circ Flow 0.2



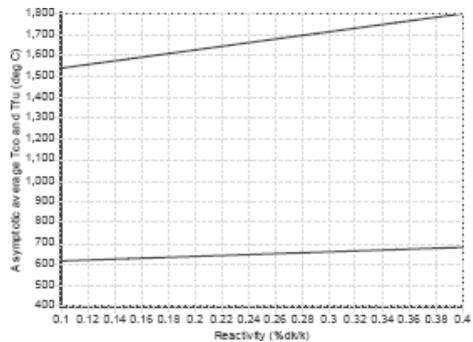
UTOP-ULOF Accident of Nitride Fuelled with  $\beta = 0.2$



UTOP-ULOF, MOX FUEL with natural Circ Flow 0.2



UTOP-ULOF, MOX FUEL with natural Circ Flow 0.2



UTOP-ULOF, MOX FUEL with natural Circ Flow 0.2

Fig 3. ULOF-UTOP Accident for MOX Fuelled Core

It is shown that for ULOF-UTOP accident for the same reactivity input for the nitride fuelled and the MOX fuelled core. It is clear that the higher the value of

reactivity the severer the accident and also the higher the natural circulation level is the better the situation. For MOX fuelled core, the natural circulation level is critical, while for nitride fuelled core the reactivity input is very critical.

### Transient Analysis with Simplified Model

In this analysis the transient model adopt point kinetic and quasistatic for the thermal hydraulic aspect. The simulation results are shown as follows

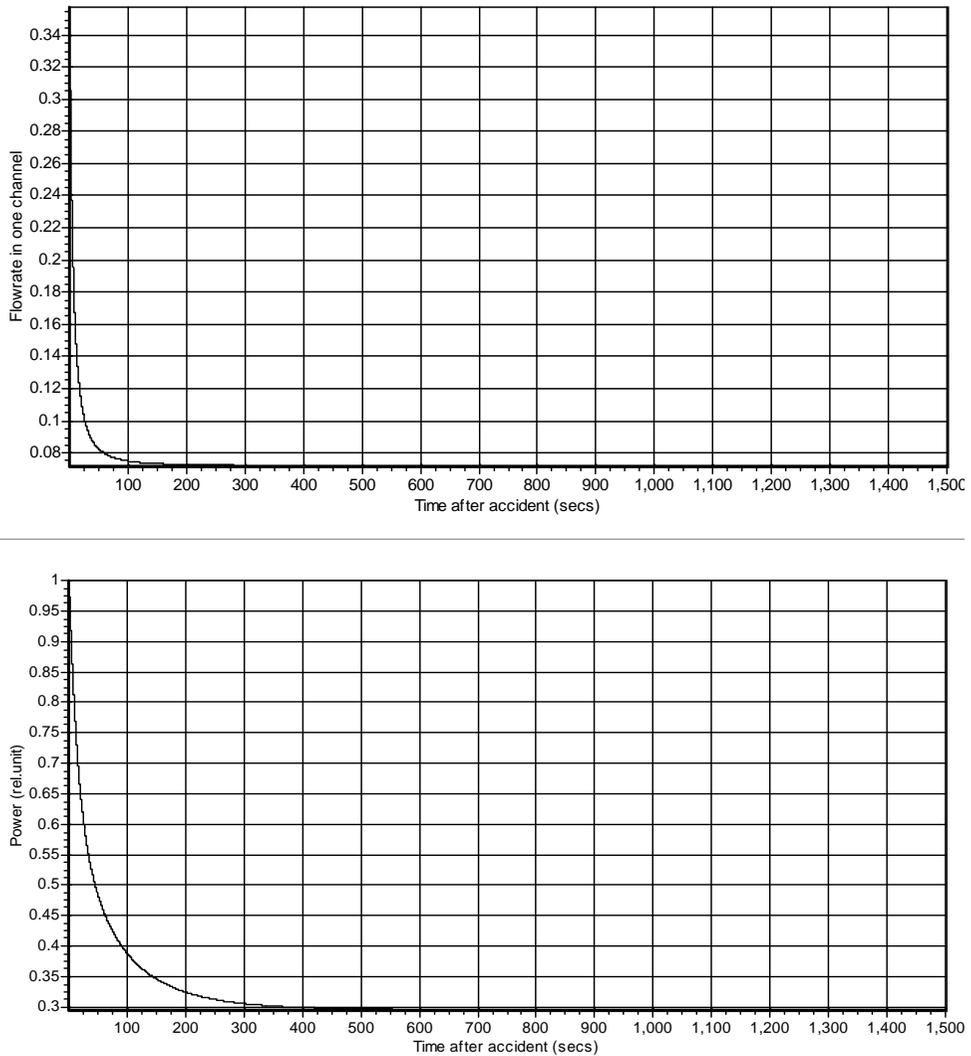


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core

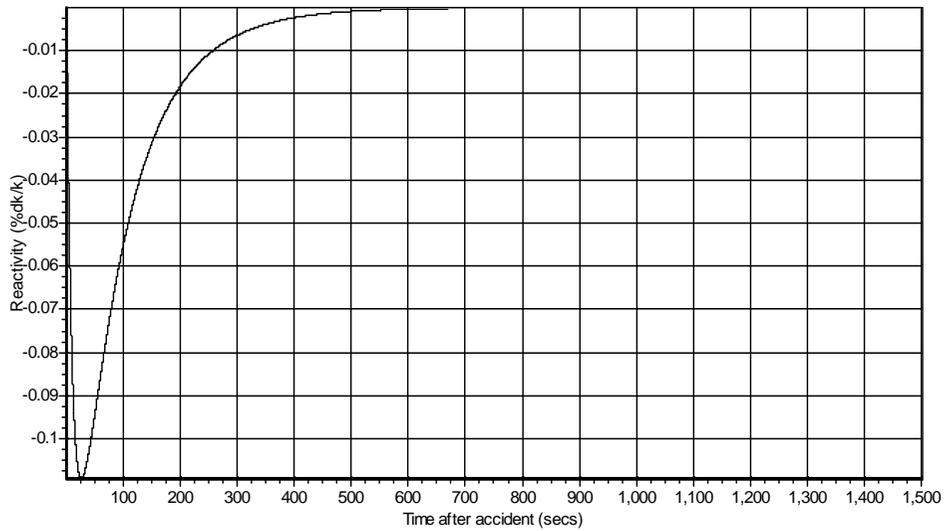
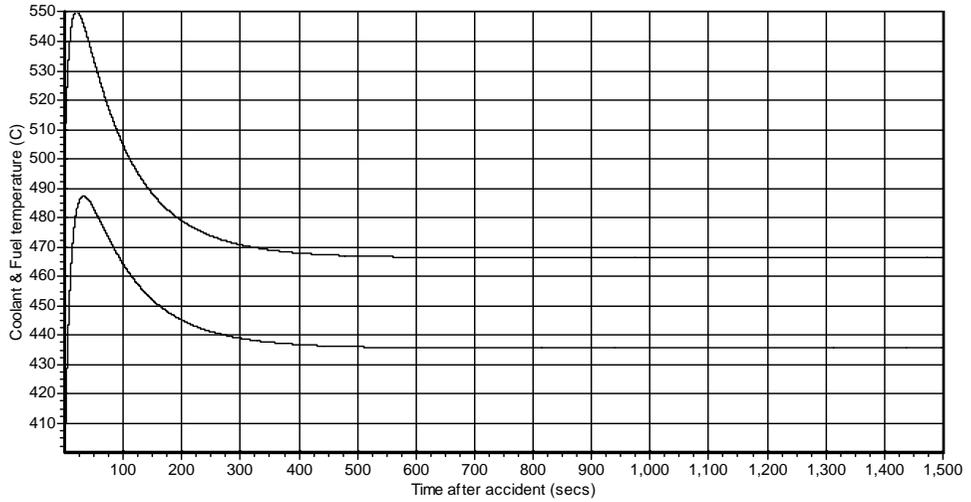


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core (continued)

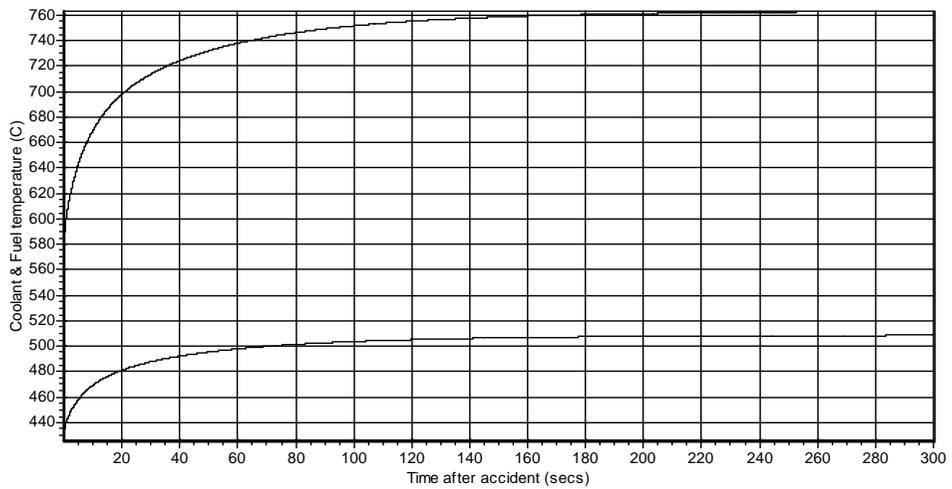
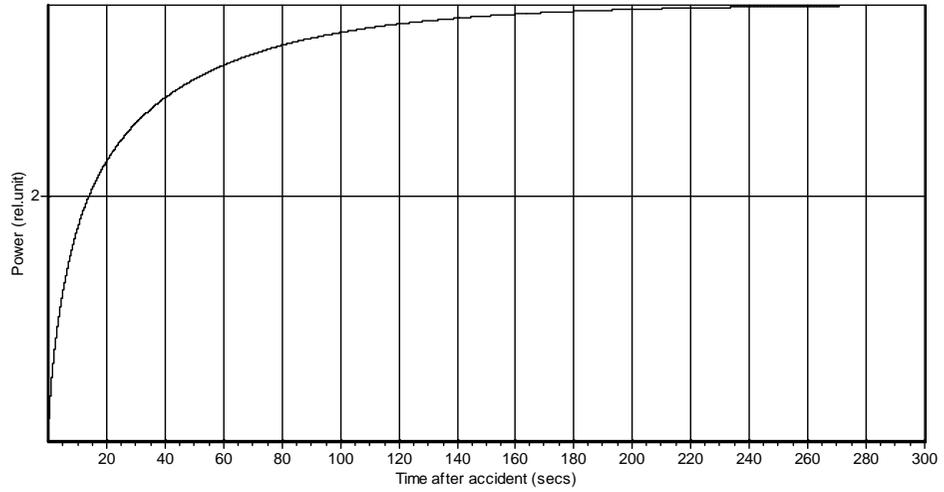


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core (continued)

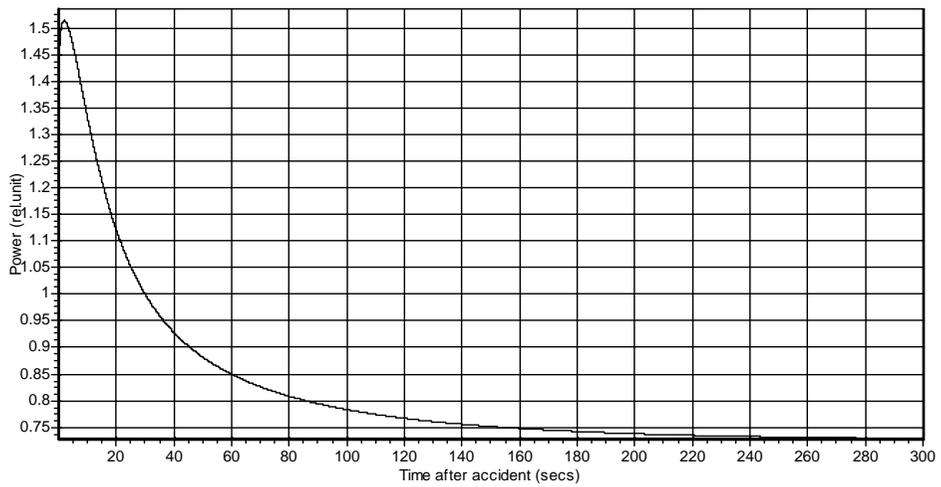
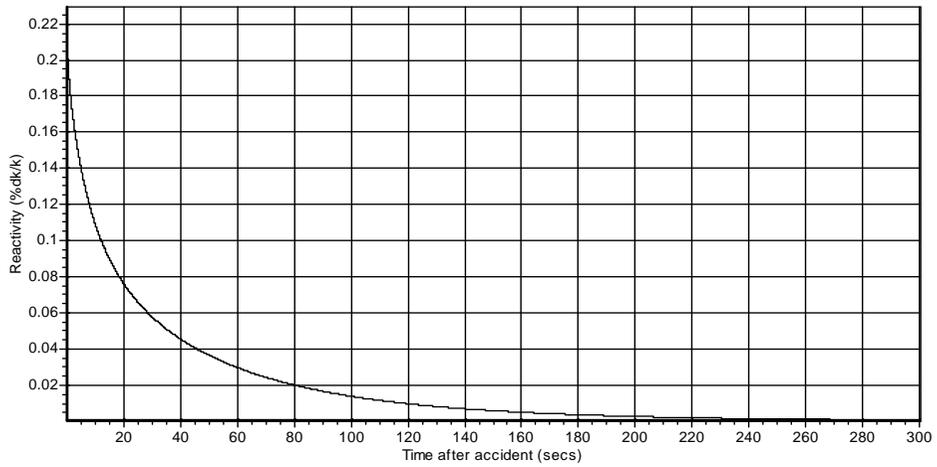


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core (continued)

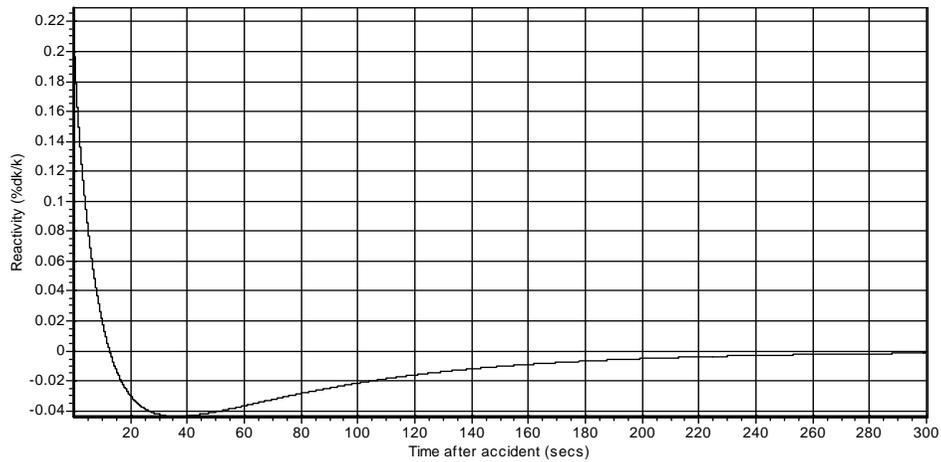
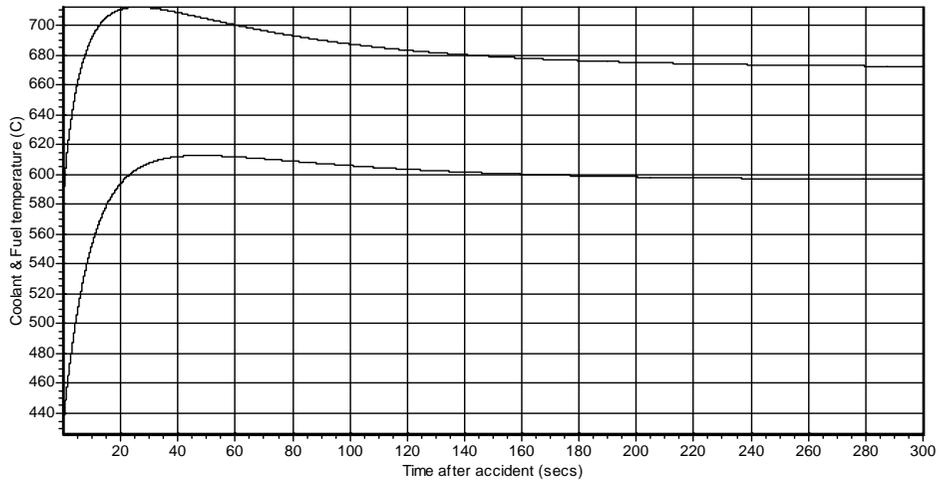


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core (continued)

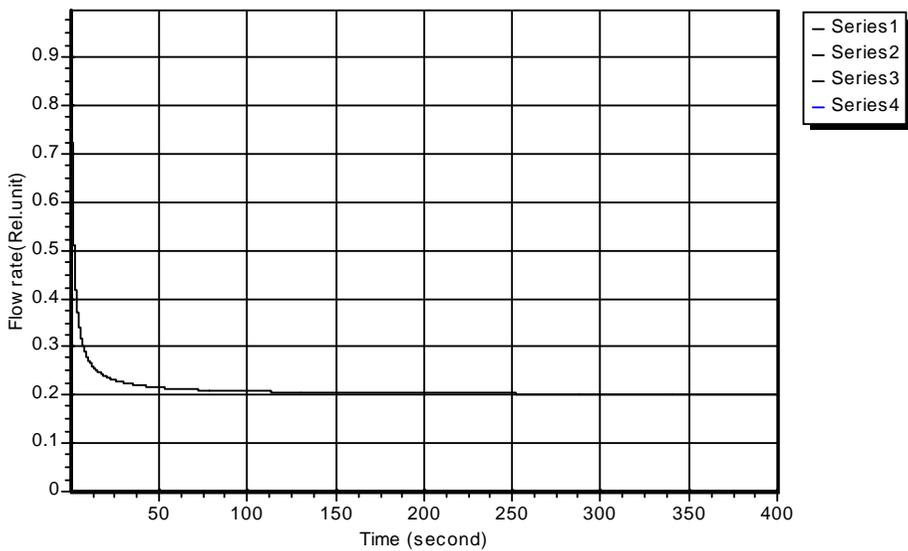
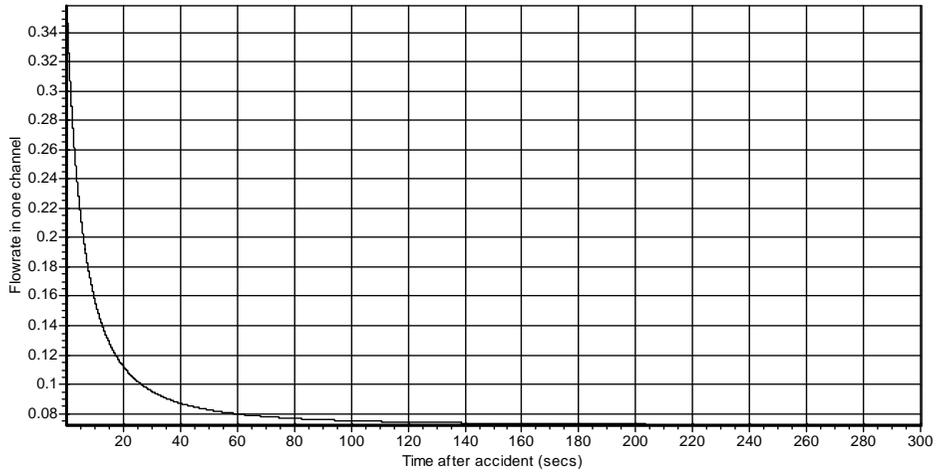


Fig. 4. The Coolant Flow Rate Change During UTOP-ULOF Accident for MOX Fuelled Core (continued)

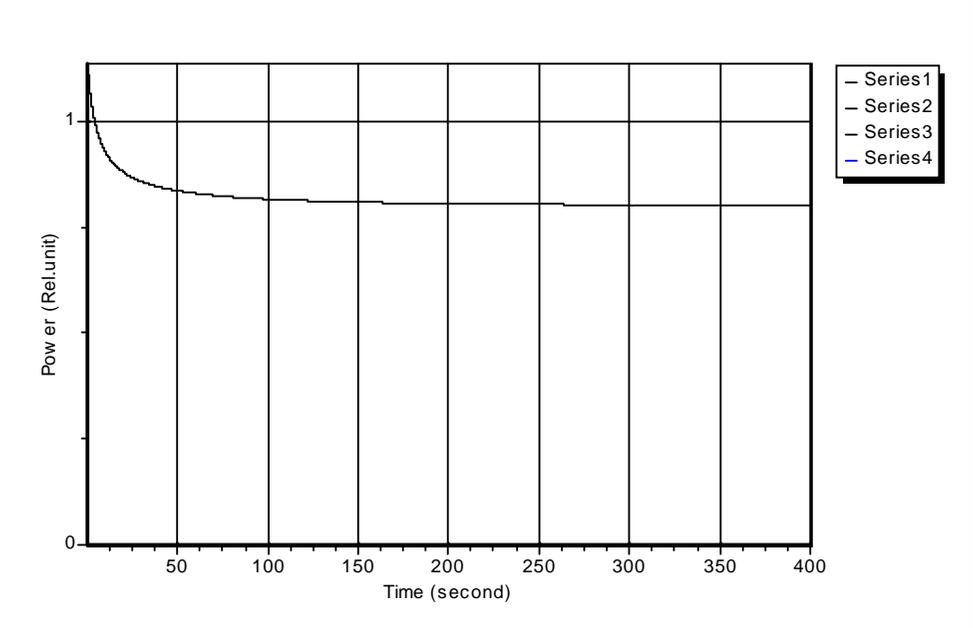


Fig. 5. The Change of Power Level with The Time for ULOF UTOP Accident with MOX Fuelled Core

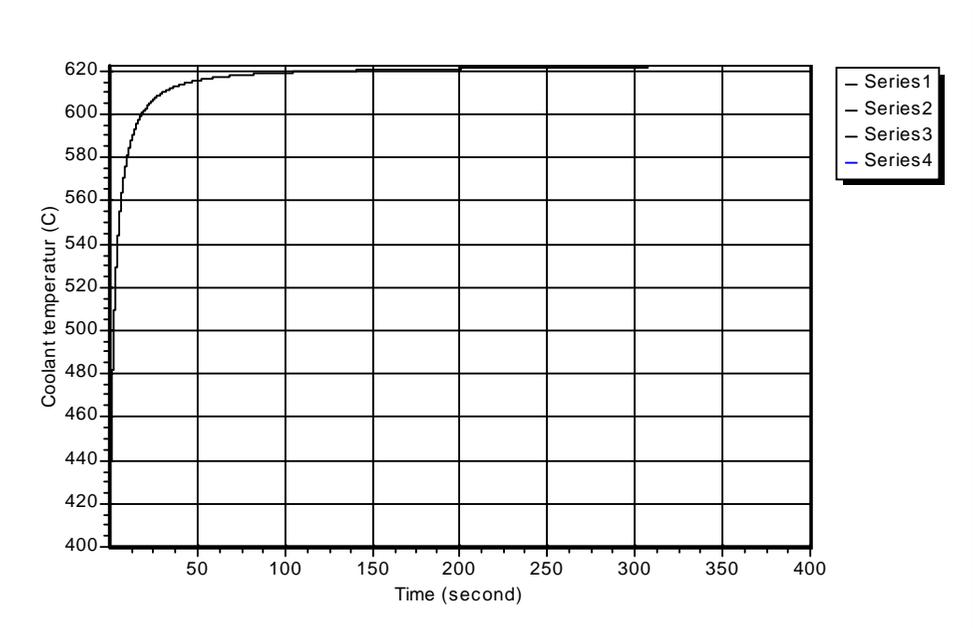


Fig. 6. The Change of Coolant Temperature with The Time for ULOF UTOP Accident with MOX Fuelled Core

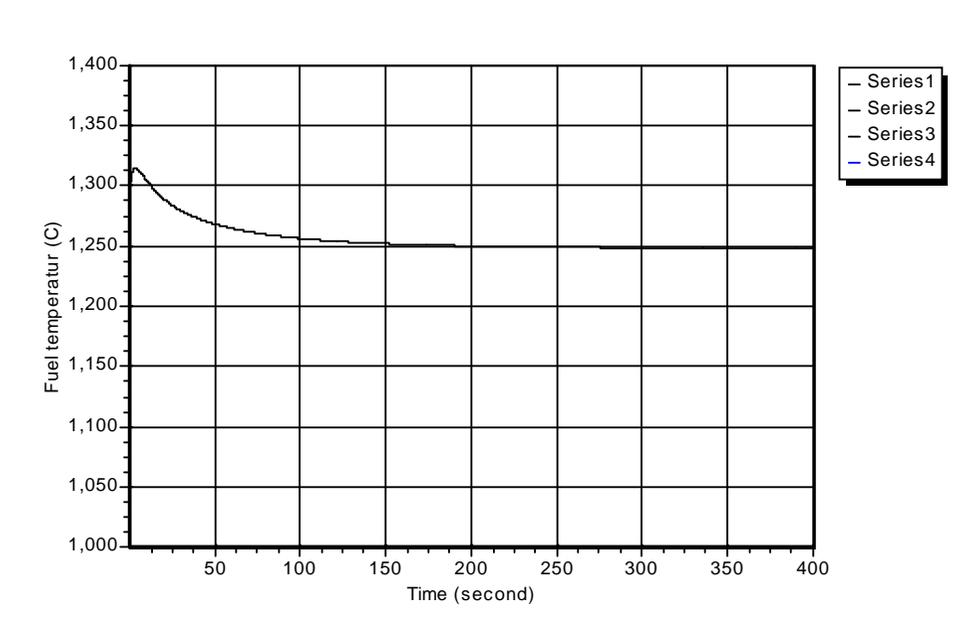


Fig 7. The Change of Fuel Temperature with The Time For ULOF UTOP Accident with MOX Fuelled Core

It is shown that coolant flow rate decreases started at  $t=0$  and go to the natural circulation level. At the same time  $0.002$  dk/k excess reactivity entered the core. It causes power and temperature increase as shown in Fig. 5, 6 and 7. This simulation was conducted with average power density of  $100$  W/cc.

Similar results also obtained for nitride fueled core which simulation results are shown in Figs.8-11. One important difference is that asymptotic power of the core is higher to the MOX fueled core due to its lower thermal conductivity characteristics.

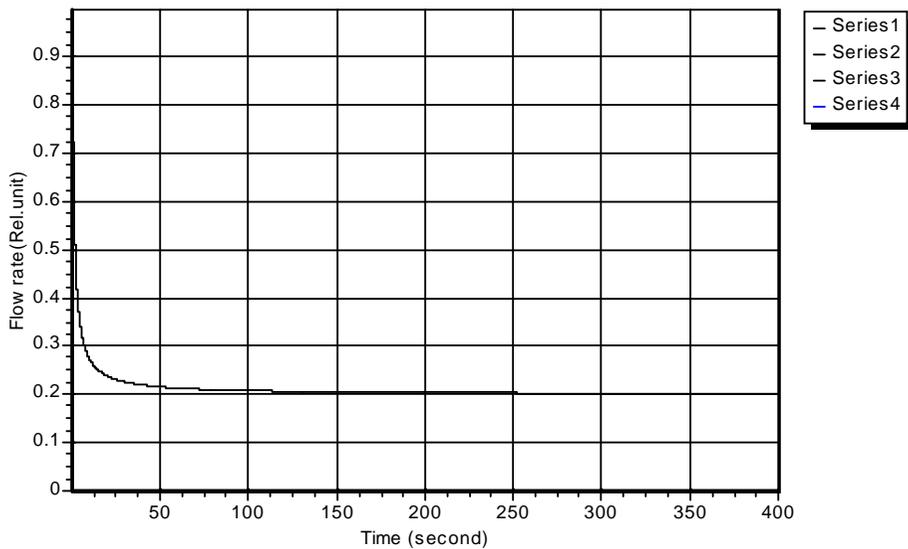


Fig. 8. The Coolant Flow Rate Change During UTOP-ULOF Accident for Nitride Fuelled Core

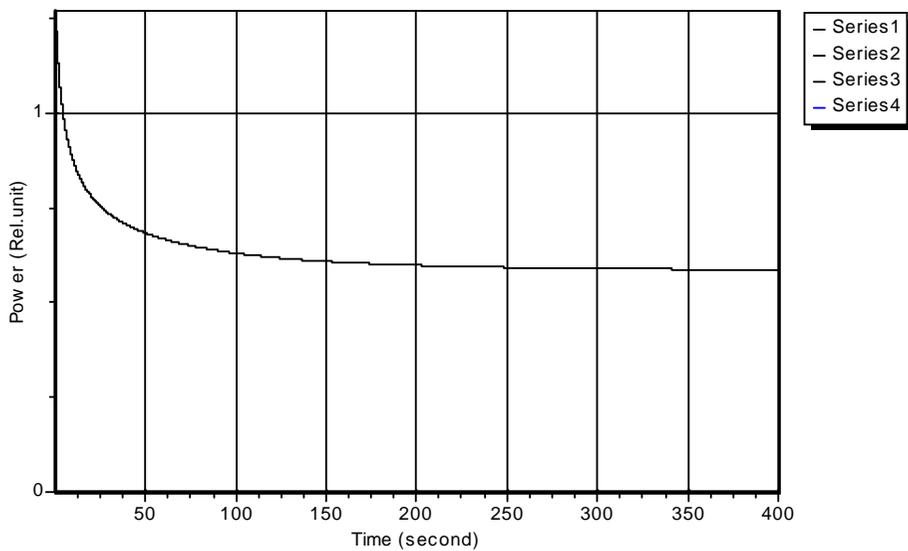


Fig. 9. The Change of Power Level with The Time for ULOF UTOP Accident with Nitride Fuelled Core

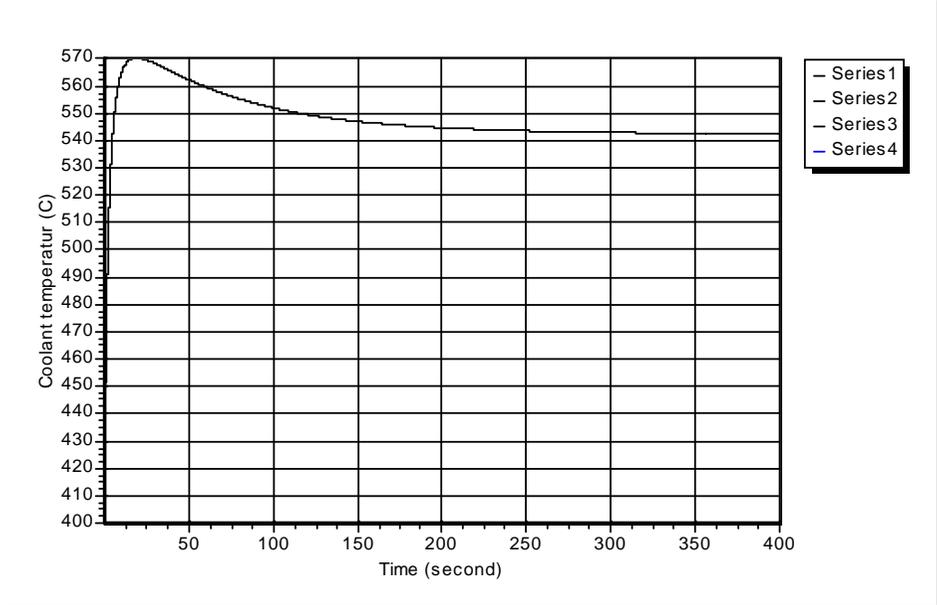


Fig. 10. The Change of Coolant Temperature with The Time for ULOF UTOP Accident with Nitride Fuelled Core

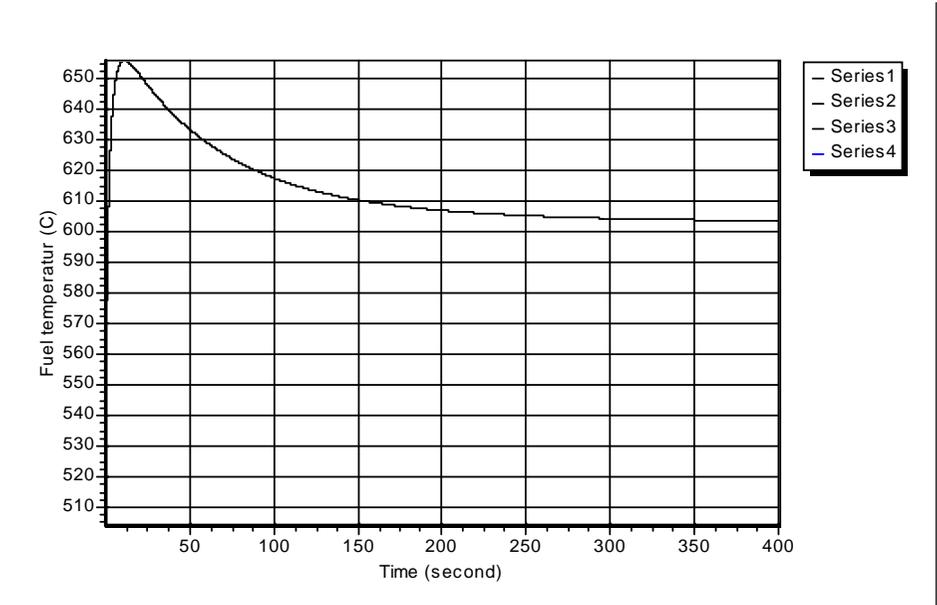


Fig 11. The Change of Fuel Temperature with The Time for ULOF UTOP Accident with Nitride Fuelled Core

### Transient in Full Scale Simulation

The full scale transient simulation in the liquid metal cooled fast reactors is described in detail at the references. The example of the results is shown as follows.

Tabel 1. Parameters for MOX FUEL 75 MWth

Parameter	Specification	
Reactor power	75MWth (~ 30 MWe)	
Average burnup	~ 10 % HM	
Peak Burnup	~ 12 % HM	
Coolant	Pb-Bi	
Shielding material	B <sub>4</sub> C + Stainless steel	
Fuel material	UO <sub>2</sub> – PuO <sub>2</sub> +additional Np237	
Fuel enrichment	9 – 13%	
Average power density	60 W/cm <sup>3</sup>	
Inlet / average outlet temperature	325°C / 450°C	
Core volume fraction		
Fuel	40-60% (inner blanket), 60% (main core)	
Structure	10 – 30 %	
Coolant	30%	
Core Size	R	Z
Inner blanket width	20 cm	20 cm
Core width	43 cm	43 cm
Reflector(coolant)	10 cm	10 cm
Shielding	40 cm	40 cm
Reactor life time	35 years continuously (without refueling and reshuffling)	
Reactivity swing	About 1\$	

We perform ULOF and UTOP simulation which the results are shown in Figs.

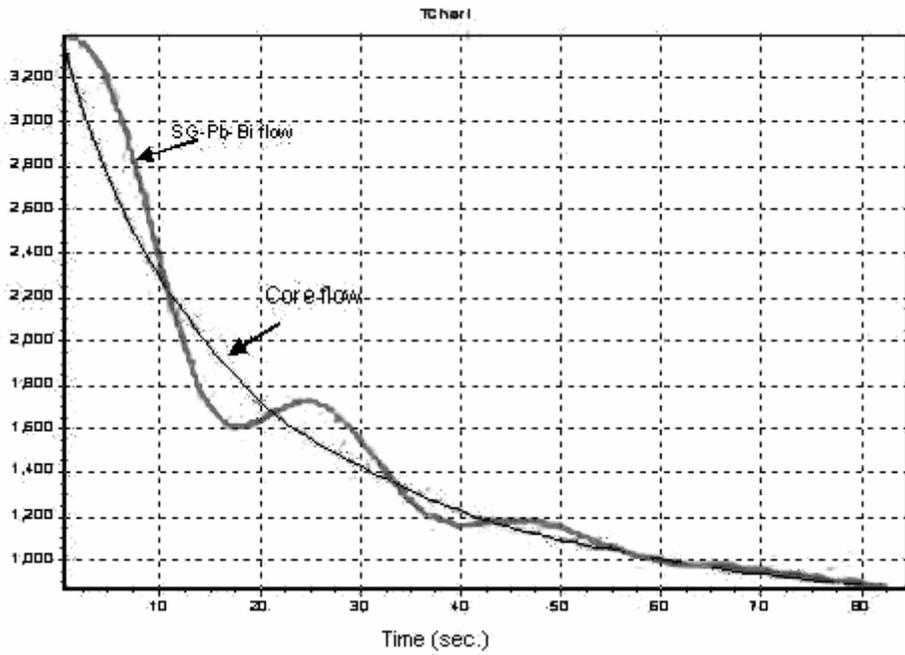


Fig. 12. The Change of Core and SG Primary Side Flow Rates with The Time for 75 MWth MOX Fueled Pb-Bi Cooled Fast Reactors Under ULOF Accidents

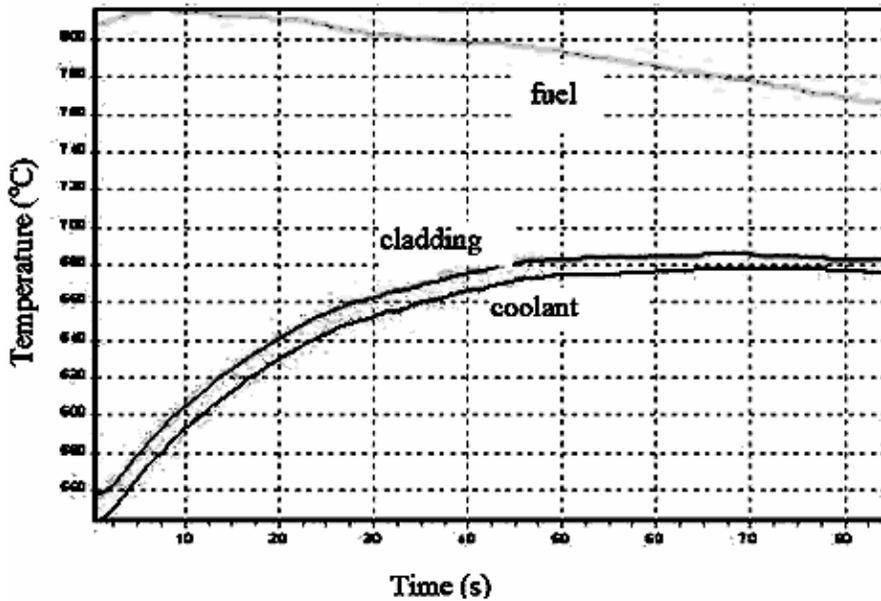


Fig. 13. The Change of Hot Spot Temperature with The Time for 75 MWth MOX Reactor During ULOF Accident

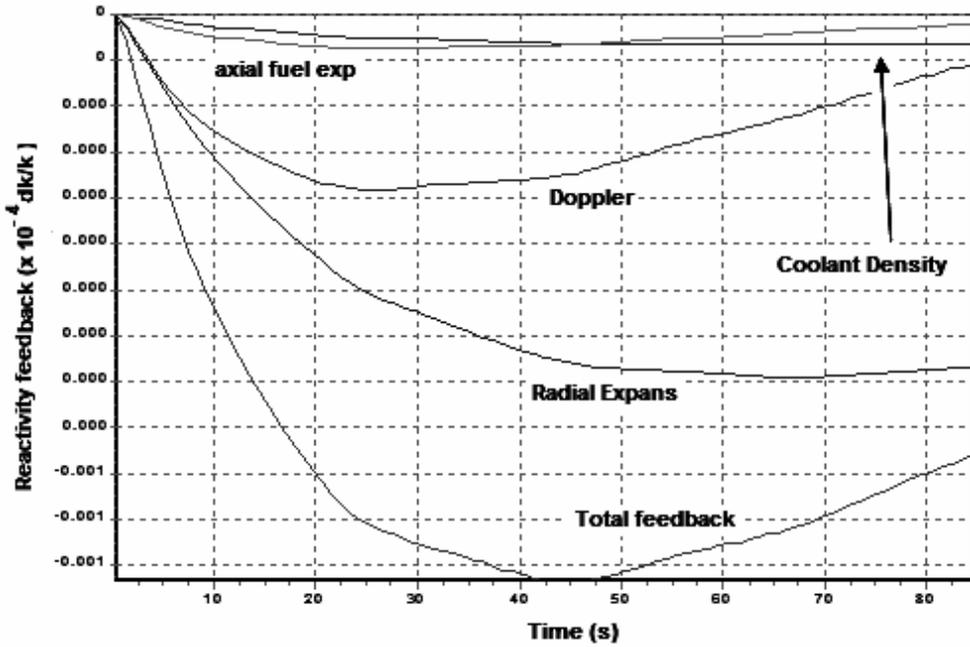


Fig. 14. The Change of Reactivity Feedback with The Time Under ULOF Accident

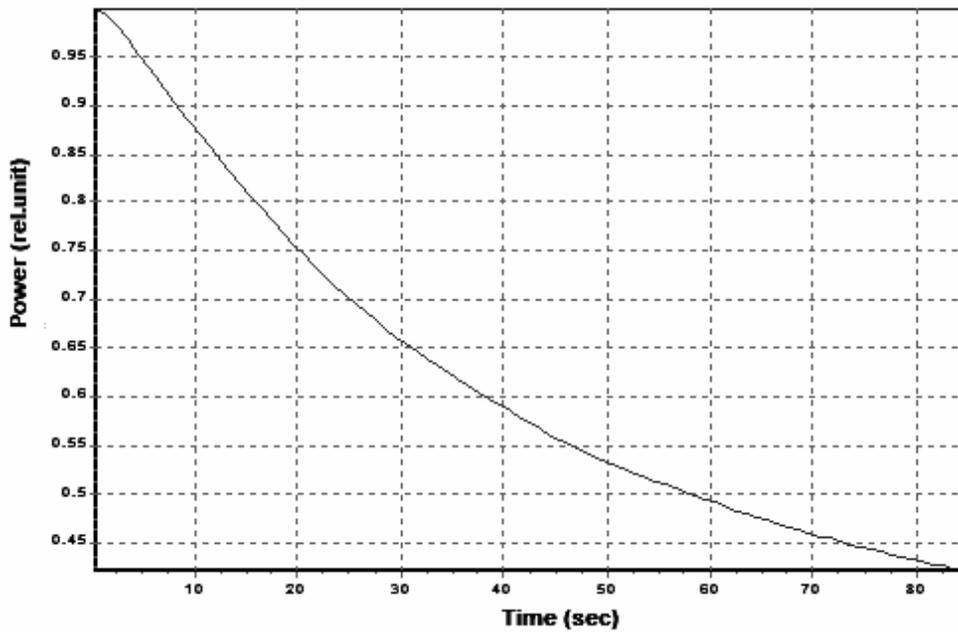


Fig. 15. The Change of Reactor Power With The Time Under ULOF Accident.

Figs. 12 to 15 show the results of the ULOF Accident. It is assumed that at  $t=0$  the pump started to loss its power so that it start to coast-down. It is also assumed that

the pump halving time is 10 seconds. Fig. 12 shows the change of coolant flow-rate during accident. It is shown that few second after the start of accident the core flow-rates and SG primary flow-rate decrease significantly toward the natural circulation level. The reduction of flow-rate causes temperature increase in coolant, cladding, and fuel pellet as shown in Fig. 13.

The increase of coolant, cladding, and fuel pellet temperature in turn cause negative feedback as shown in Fig. 14. It is shown that Radial expansion and Doppler reactivity feedback are important to create negative feedback to reduce the power level so that the system can move toward new equilibrium condition.

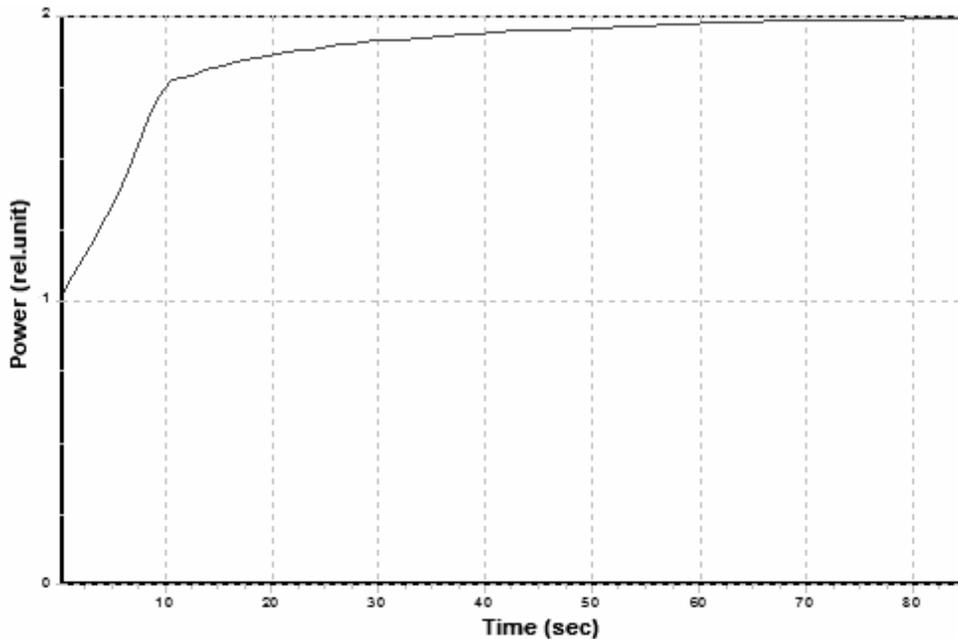


Fig. 16 The Change of Reactor Power With The Time For 75 Mwth MOX Fueled Pb-Bi Cooled Fast Reactors Under UTOP Accident.

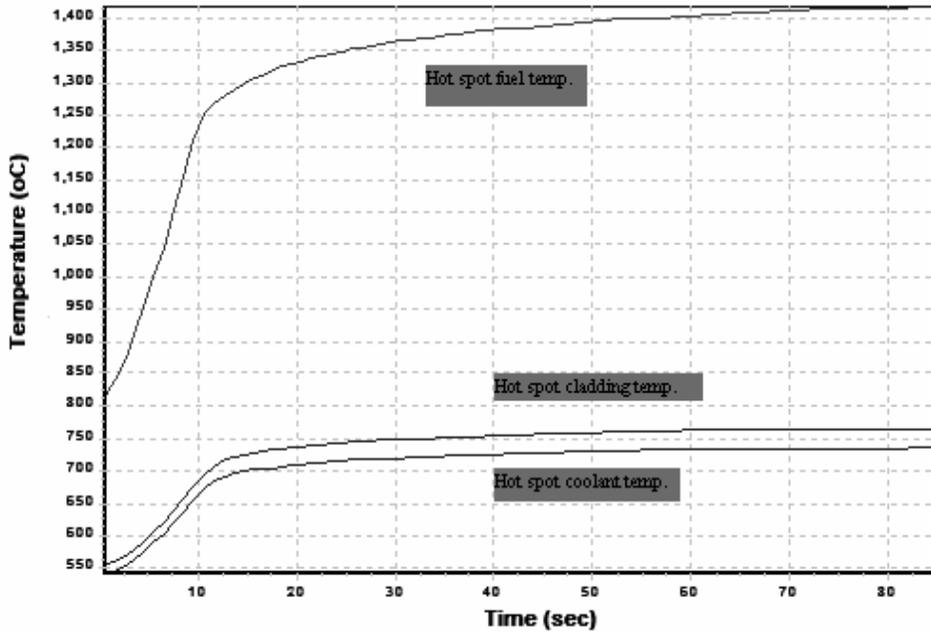


Fig. 17. The Change of Hot Spot Coolant, Cladding and Fuel Temperature During UTOP Accident

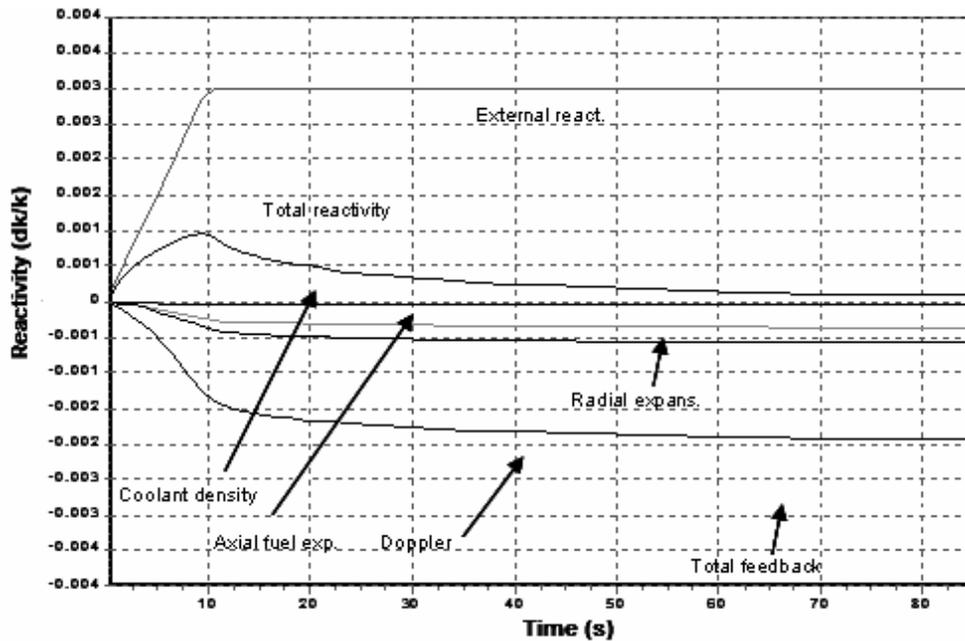


Fig. 18 The Change of Reactivity Feedback With The Time During UTOP Accident

Figs. 16, 17 and 18 show the simulation results of UTOP accident. It is assumed that a rather large reactivity input that is 0.3%dk/k positive external reactivity is introduced linearly during 10 seconds. Finally the system reach new equilibrium condition with elevated power level thank to enough Doppler and Radial expansion feedback to compensate the external reactivity.

Therefore Doppler and fuel axial reactivity feedback is more important in UTOP case than in ULOF case. It is shown that this reactor can survive 0.3% external reactivity inherently.

### Conclusion

Accident analysis for liquid metal cooled fast reactors with various level of complexity/accuracy has been developed. Asymptotic model is very useful in the study of general safety performance especially the inherent safety characteristics globally. This method is useful for inherent safety introduction for undergraduate students.

The transient simulation with simplified model is useful to simulate long term behaviour of the system under a certain accident condition which need long term simulation. It is also useful for nuclear education. The full scale simulation is useful for real NPP design simulation and for master student and doctoral student research.

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